

Relative Clauses
LING 553
February 18-20, 2008

1. SIMPLE RELATIVE CLAUSES

- (1) The college that is in Hanover is famous.¹ \equiv “Dartmouth is famous”

We want “the college that is in Hanover” to denote Dartmouth. So “college that is in Hanover” should denote {Dartmouth}.

This is easy, if not mindless:

- **[[college that is in Hanover]]** = **[[college in Hanover]]** = $\lambda x_e . x$ is a college and x is in Hanover

- (2) The college that enrolled Robert Frost is in Hanover.

Again, this can be fairly straightforward:

- **[[college that graduated Robert Frost]]**:
[[college]] = $\lambda x_e . x$ is a college
[[graduated Robert Frost]] = $\lambda x_e . x$ graduated Robert Frost
...once again, use Predicate Modification

2. HARDER RELATIVE CLAUSES

- (3) The college [that Robert Frost attended] is in Hanover.

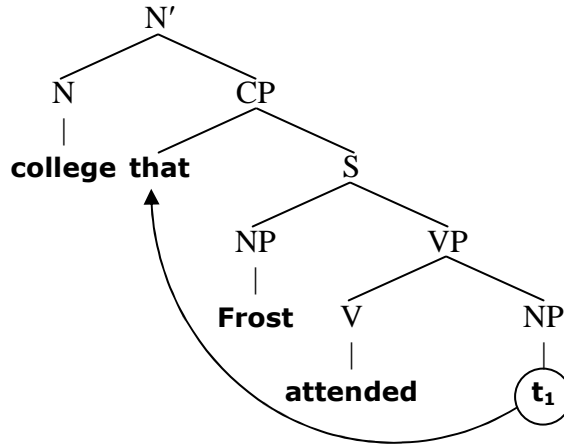
- **[[college that Robert Frost attended]]**:
[[college]] = $\lambda x_e . x$ is a college
[[Robert Frost attended]] = $\lambda x_e . x$ attended Robert Frost ← WRONG!

What can we do?

¹ We'll take “Hanover” to denote Hanover, New Hampshire. There's only one college there.

2.1. A First Revision of Our System

Answer: *movement* and *traces*.



Because $\llbracket \text{attended} \rrbracket$ has type $\langle e, \langle e, t \rangle \rangle$, the trace must denote something of type e .

Or, at Aaron's suggestion, something higher. See appendix.

Suppose it's an arbitrary variable over individuals: x . Then working bottom-up:

$$\llbracket \mathbf{t_1} \rrbracket = x$$

$$\llbracket \text{attended} \rrbracket = [\lambda z_e . \lambda y_e . y \text{ attended } z]$$

$$\llbracket \text{attended } \mathbf{t_1} \rrbracket = [\lambda z_e . \lambda y_e . y \text{ attended } z](x) = [\lambda y_e . y \text{ attended } x]$$

$$\llbracket \text{Frost attended } \mathbf{t_1} \rrbracket = [\lambda y_e . y \text{ attended } x](\text{Frost}) = \text{Frost attended } x$$

And working top-down, we want:

$$\llbracket \text{college that Frost attended } \mathbf{t_1} \rrbracket = \lambda x_e . x \text{ is a college and Frost attended } x$$

$$\llbracket \text{that Frost attended } \mathbf{t_1} \rrbracket = \lambda x . \text{Frost attended } x$$

So it looks like the relative pronoun **that** means “put a λx in front”. That's a new rule of composition for us:

(4) **The Rule of Function Abstraction** (or λ -abstraction) – first draft

If we have a node α , and its daughters are β and a relative pronoun, then $\llbracket \alpha \rrbracket = [\lambda x . \llbracket \beta \rrbracket]$.

Except that...how did we know to put an x in there? We could look into the inner workings of β , but it's better to avoid doing that kind of thing.

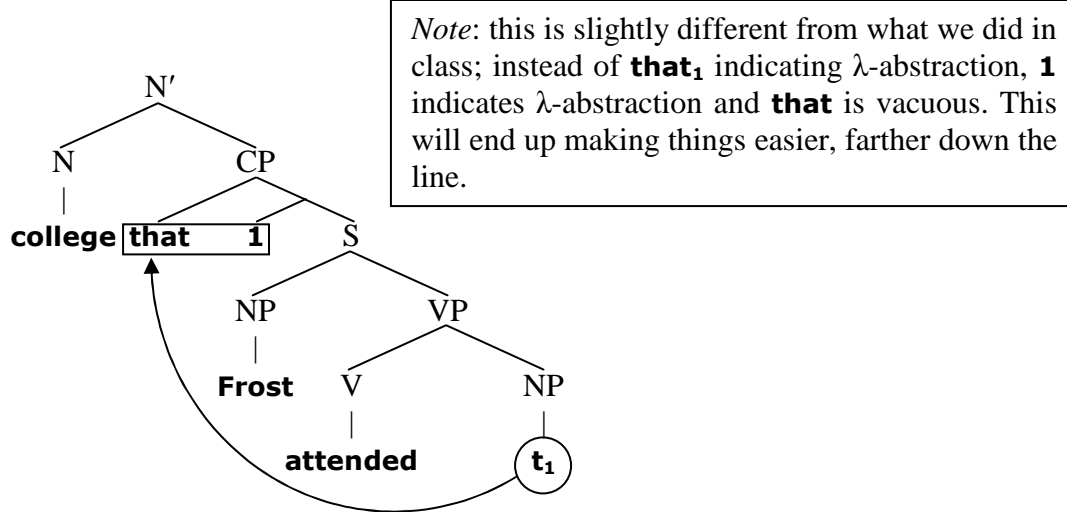
Moreover: **such that Frost attended it** has roughly the same meaning as **that Frost attended t_1** , so if $\llbracket \mathbf{it} \rrbracket = \llbracket \mathbf{t}_1 \rrbracket = x$, then we're fine...until we have

$\llbracket \mathbf{the\ college\ such\ that\ I\ read\ the\ book\ that\ } t_1 \mathbf{\ is\ about\ it} \rrbracket =$

“the unique x where x is a college and I read the unique x where x is a book and x is about x ”, and boy is that wrong. (The unique thing that's both a book and about itself?)

2.2. A Re-Revision of Our System

What we really need is a way of keeping track of which variable is which. So let's number our traces and pronouns, i.e. “index” them.



All right, but:

- What do the numbers mean?
- What does t mean?

Instead of having t_1 denote an arbitrary individual, we'll have it denote “individual number one”. Then:

(5) The Rule of λ -Abstraction – second draft

If we have a node α , and its daughters are β and an index n , then $\llbracket \alpha \rrbracket = [\lambda x_n . \llbracket \beta \rrbracket]$.

That gives:

$$\llbracket \mathbf{t}_1 \rrbracket = x_1$$

$$\llbracket \mathbf{attended} \rrbracket = [\lambda z_e . \lambda y_e . y \text{ attended } z]$$

$$\llbracket \mathbf{attended } t_1 \rrbracket = [\lambda z_e . \lambda y_e . y \text{ attended } z](x_1) = [\lambda y_e . y \text{ attended } x_1]$$

$$\llbracket \mathbf{Frost attended } t_1 \rrbracket = [\lambda y_e . y \text{ attended } x_1](\text{Frost}) = \text{Frost attended } x_1$$

$$\llbracket \mathbf{1 Frost attended } t_1 \rrbracket = \lambda x_1 . \llbracket \mathbf{Frost attended } t_1 \rrbracket = \lambda x_1 . \text{Frost attended } x_1$$

Which is what we wanted.

2.3. One More Revision of Our System

...sort of. How do we know who “individual number one” is? And what if we’d chosen \mathbf{t}_{23} ?
 What we need is a way to assign individuals to numbers. So:

(6) *Assignments*

An assignment function is a function $g : \{\text{integers}\} \rightarrow D_e$.

Some sample assignment functions:

$$g = \begin{bmatrix} 1 \rightarrow \text{George W. Bush} \\ 2 \rightarrow \text{Beatrice Santorini} \\ 3 \rightarrow \text{Dartmouth} \\ \vdots \\ 23 \rightarrow \text{Michael Jordan} \\ 24 \rightarrow \text{Michael Jackson} \\ 25 \rightarrow \text{Mary Jane Watson} \\ \vdots \end{bmatrix} \qquad g' = \begin{bmatrix} 1 \rightarrow \text{Michael Jackson} \\ 2 \rightarrow \text{Michael Jackson} \\ 3 \rightarrow \text{Michael Jackson} \\ \vdots \\ 23 \rightarrow \text{Michael Jackson} \\ 24 \rightarrow \text{Michael Jackson} \\ 25 \rightarrow \text{Michael Jackson} \\ \vdots \end{bmatrix}$$

We also need to say that trees are interpreted relative to assignment functions:

(7) *The interpretation function*

A tree α is in the domain of $\llbracket \dots \rrbracket$ iff, for all assignment functions g, g' : $\llbracket \alpha \rrbracket^g = \llbracket \alpha \rrbracket^{g'}$.
 If α is in the domain of $\llbracket \dots \rrbracket$, then for all assignment functions g , $\llbracket \alpha \rrbracket = \llbracket \alpha \rrbracket^g$.

...and that the meaning of a trace (or pronoun) is determined by the index, while the meaning of other things is assignment-function-independent:

(8) *The meaning of traces and pronouns*

- a. If α is a trace with index i , then $\llbracket \alpha \rrbracket^g = g(i)$.
- b. If α is a pronoun with index i , then $\llbracket \alpha \rrbracket^g = g(i)$.

That’ll get us most of the way through a tree. Now we have:

$$\begin{aligned} \llbracket \mathbf{t}_1 \rrbracket^g &= g(1) \\ \llbracket \mathbf{attended} \rrbracket &= [\lambda z_e . \lambda y_e . y \text{ attended } z] \\ \llbracket \mathbf{attended t}_1 \rrbracket^g &= \llbracket \mathbf{attended} \rrbracket^g(\llbracket \mathbf{t}_1 \rrbracket^g) = \llbracket \mathbf{attended} \rrbracket(\llbracket \mathbf{t}_1 \rrbracket^g) \\ &= [\lambda z_e . \lambda y_e . y \text{ attended } z](g(1)) = [\lambda y_e . y \text{ attended } g(1)] \\ \llbracket \mathbf{Frost attended t}_1 \rrbracket^g &= [\lambda y_e . y \text{ attended } g(1)](\text{Frost}) = \text{Frost attended } g(1) \end{aligned}$$

Of course, $\llbracket \mathbf{Frost\ attended\ t_1} \rrbracket$ is undefined. Why? Because, if we use the g, g' above:

$$\begin{aligned} \llbracket \mathbf{Frost\ attended\ t_1} \rrbracket^g &= \text{Frost attended } g(1) = \text{Frost attended George W. Bush} \\ \llbracket \mathbf{Frost\ attended\ t_1} \rrbracket^{g'} &= \text{Frost attended } g'(1) = \text{Frost attended Michael Jackson} \end{aligned}$$

which means that its meaning isn't the same for all assignment functions.

What we want at this point is a way to say, "Whatever assignment function we're using, I'll modify it so that it always maps '1' to the same individual, say, George W. Bush. That way, **Frost attended t_1** will always mean 'Frost attended George W. Bush', independent of the particular assignment function I started with."

(9) *Modified assignments*

If g is an assignment function, then $g[i \rightarrow x]$, also written $g^{x/i}$, is the assignment function h such that:

- (i) $h(i) = x$, and
- (ii) for all integers $j \neq i$, $h(j) = g(j)$.

How does *that* help? Well:

(10) **The Rule of λ -Abstraction (rule #3)**

If α has daughters β, γ , where β is an index i ,
 then for any assignment function g , $\llbracket \alpha \rrbracket^g = \lambda x : x \in D_e . \llbracket \gamma \rrbracket^{g[i \rightarrow x]}$

Putting this to work:

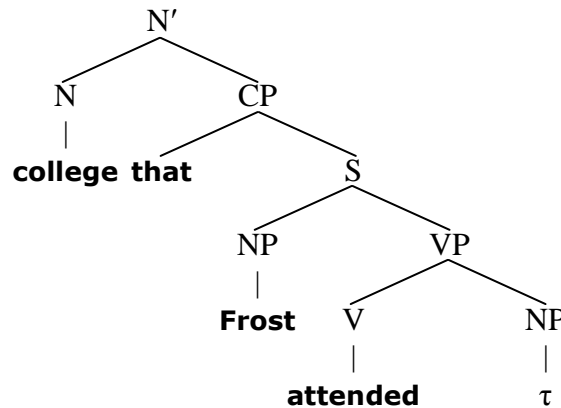
$$\begin{aligned} &\llbracket \mathbf{1\ Frost\ attended\ t_1} \rrbracket^g \\ &= \lambda x : x \in D_e . \llbracket \mathbf{Frost\ attended\ t_1} \rrbracket^{g[1 \rightarrow x]} \\ &= \lambda x : x \in D_e . \llbracket \mathbf{attended} \rrbracket^{g[1 \rightarrow x]} (\llbracket \mathbf{t_1} \rrbracket^{g[1 \rightarrow x]})(\llbracket \mathbf{Frost} \rrbracket^{g[1 \rightarrow x]}) \\ &= \lambda x : x \in D_e . \llbracket \mathbf{attended} \rrbracket(\llbracket \mathbf{t_1} \rrbracket^{g[1 \rightarrow x]})(\llbracket \mathbf{Frost} \rrbracket) \\ &= \lambda x : x \in D_e . [\lambda z_e . \lambda y_e . y\ \text{attended}\ z](g[1 \rightarrow x](1))(\text{Frost}) \\ &= \lambda x : x \in D_e . [\lambda z_e . \lambda y_e . y\ \text{attended}\ z](x)(\text{Frost}) \\ &= \lambda x : x \in D_e . \text{Frost attended } x \end{aligned}$$

Which is what we wanted.

3. APPENDIX: AARON'S τ

If there's an invisible τ with a higher meaning, could it take **[[attended]]** as an argument and return something that can take **[[Frost]]** and put it into the subject position?

Answer: sure...



$[[\tau]] = \lambda R : R \in D_{\langle e, \langle e, t \rangle \rangle} . \lambda x : x \in D_e . \lambda y : y \in D_e . [R(y)(x)]$. This gives:

$$[[\text{attended}]] = [\lambda x_e . \lambda y_e . y \text{ attended } x]$$

$$\begin{aligned}
 [[VP]] &= [[\tau]]([\text{attended}]) \\
 &= [\lambda R_{\langle e, \langle e, t \rangle \rangle} . \lambda x_e . \lambda y_e . [R(y)(x)]](\lambda x_e . \lambda y_e . y \text{ attended } x) \\
 &= [\lambda R_{\langle e, \langle e, t \rangle \rangle} . \lambda x_e . \lambda y_e . [R(y)(x)]](\lambda u_e . \lambda v_e . v \text{ attended } u) \\
 &= \lambda x_e . \lambda y_e . [[\lambda u_e . \lambda v_e . v \text{ attended } u](y)(x)] \\
 &= \lambda x_e . \lambda y_e . [[\lambda v_e . v \text{ attended } y](x)] \\
 &= \lambda x_e . \lambda y_e . x \text{ attended } y
 \end{aligned}$$

...which is **[[attended]]** with its arguments reversed. (Exercise: verify for yourself that this gives the right meaning for **college that Frost attended**.)

3.1. Problems

Why not do things this way?

- It's awfully powerful. Can we ensure that τ doesn't show up unexpectedly in trees, so that we actually have **Booth shot τ Lincoln**, with the meaning "Lincoln shot Booth"?
- The "gap" that the τ needs to fill happens to be in the object position of a transitive verb; but it can go elsewhere, e.g. indirect object position, subject position.... How many τ s do we need?
- Are pronouns also τ ? If so, does [the college such that I read a book that τ is about τ] work, or do we end up needing to somehow "index" each τ ?