

Homework 4
LING 255
Due: March 6, 2008

1. THE ASSIGNMENT

For each of the following sentences (trees appear on the next page), either:

- Write out a step-by-step derivation that shows what interpretation the sentence receives (and indicate whether that interpretation is correct), *or*
- Indicate clearly why such a derivation is not possible without changing the theoretical assumptions laid out in the next section.

- (1) Every bearded student shaves.
- (2) Every student who is bearded shaves.
- (3) Every student likes the president of Penn.
- (4) The president of Penn likes every student.

2. THE THEORETICAL ASSUMPTIONS

2.1. Meanings

[[every]] $\lambda P : P \in D_{\langle e, t \rangle} . \lambda Q : Q \in D_{\langle e, t \rangle} . \{x \mid P(x) = \text{TRUE}\} \subseteq \{y \mid Q(y) = \text{TRUE}\}$
[[the]] $\lambda P : P \in D_{\langle e, t \rangle}$ and P is a singleton set . the only $x \in D_e$ such that $P(x) = \text{TRUE}$

[[president]] $\lambda x : x \in D_e . \lambda y : y \in D_e . y$ is a president of x

[[likes]] $\lambda x : x \in D_e . \lambda y : y \in D_e . y$ likes x

[[bearded]] $\lambda x : x \in D_e . x$ is bearded

[[shaves]] $\lambda x : x \in D_e . x$ shaves

[[student]] $\lambda x : x \in D_e . x$ is a student

[[Penn]] the University of Pennsylvania

who, is, of: semantically vacuous, and can be ignored.

2.2. Composition Rules

Function Application (Rule #1 of Interpretation)

If a node M has daughters D_1, D_2 , and D_1 is a function that can take D_2 as an argument, then $[[M]] = [[D_1]]([[D_2]])$

Predicate Modification (Rule of Interpretation #2)

If a node M has daughters D_1, D_2 , and $\llbracket D_1 \rrbracket$ and $\llbracket D_2 \rrbracket$ both have the semantic type $\langle e, t \rangle$, then $\llbracket M \rrbracket = [\lambda x : x \in D_e . \text{TRUE iff } \llbracket D_1 \rrbracket(x) = \text{TRUE and } \llbracket D_2 \rrbracket(x) = \text{TRUE}]$.

Vacuous Meaning (Rule of Interpretation #3)

If a node M has daughters D_1, D_2 , and D_1 is vacuous, then $\llbracket M \rrbracket = \llbracket D_2 \rrbracket$.

2.3. Trees

