## Productivity \& Paradigmatic Gaps

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## stride-strode-*strode/???stridden

|  | BNC | COCA |  | BNC | COCA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ride | 1607 | 10904 | stride | 102 | 402 |
| rides | 230 | 2495 | strides | 54 | 682 |
| riding | 1696 | 10994 | striding | 253 | 715 |
| rode | 1079 | 5997 | strode | 641 | 1752 |
| *rided | 1 | 0 | *strided | 0 | 2 |
| ridden | 456 | 1303 | *stridden | 1 | 2 |

$$
\boldsymbol{p}=1.6 \mathrm{e}-37 \boldsymbol{p}=1.5 \mathrm{e}-295
$$

From COCA (1990-2005) (1)... while Angela has stridden into the country
(2) ... And he'd shattered the screen of his monitor with one kick of his oaken legs, hauled open the steel door normally used only by Ted, and stridden into the Grim Reaper personally

## you say "stridden"? more later!

## When language fails

- Halle (1973): Some $75^{+}$Russian verbs, all in the 2 nd conjugation, do not have a first person singular non-past form
- *lažu 'I climb’
- *pobežu/*pobeždu 'I conquer'
- *deržu 'I talk rudely'
- *mužu 'I stir up’
- *erunžu 'I behave foolishly'
+: Sims (2006, OSU Dissertation)


## How language succeeds

- Sapir (1928: 37-38) "the fact of grammar, a universal trait of language, ... a generalized expressions of the feelings that analogous concepts and relations are most conveniently symbolized in analogous form ... All grammars leak"
- Chomsky \& Halle (1968: 172) "Clearly, we must design our linguistic theory in such a way that the existence of exceptions does not prevent the systematic formulation of those regularities that remain."
- Language is productive but not in an obvious way
- English words are overwhelmingly stress initial (86-90\% token, $80 \%$ type in CHILDES input; Legate \& Yang 2012) but English does not have a QI metrical system


## Outline

- A model of learning productive processes (Yang 2002, 2005, 2010)
- Failure to reach productivity leads to gaps (Halle 1973, esp. fn 1)
- Five case studies: English past tense, amn't, Spanish, Polish and Russian


## Productivity is Categorical



This is a man who knows how to GLING. He is GLINGING. He did the same thing yesterday. What did he do yesterday? Yesterday he $\qquad$

- Only one out of 86 children produced bing-bang, gling-glang (Berko 1958)
- Over-regularization (holded): $\mathbf{8 - 1 0 \%}$
- Over-irregularization (brang): $<\mathbf{0 . 2 \%}$
- Xu \& Pinker (1995): many are t/d deletion.
- Strongly confirmed cross-linguistically (Guasti 2002)
- Rating studies (e.g., Albright \& Hayes 2002) can be misleading (Gleitman et al. 1983)
- But -ed forms of pseudo-irregulars are consistently rated better (Pinker \& Prasada 1991)
- Schütze (2005), Yang (2008)


## Tolerating Exceptions

- The child has learned only two words: sing-sang, \& ring-rang
- $/ \mathrm{i} \rightarrow \mathrm{a} /$
- Exceptions accumulate as vocabulary grows
- bring, sting, swing, wing, etc., and the rule $/ \mathrm{i} \rightarrow \mathrm{a} /$ stops working so well (cf., "add -d" fails on only about 150 words)
- How many exceptions are "too many"?
- not statistical summary of the data (Albright \& Hayes 2002, Baayen 1993, etc.)


## Theory $\Rightarrow$ Processing $\Rightarrow$ Learning

## - Exception 1 - Exception 2 - Exception 3 <br> -Rule

- Exceptions exhibit frequency effects: this can be formalized as a ranked-list (Forster 1976, Murray \& Forster 2004)
- Crucially, rule-following items would have to wait to be processed after the exceptions are checked
- You should be skeptical!


## Measuring Rules

- Exceptions are faster than Rules (when suitably matched in frequencies)
- Grammaticality judgment on the fly: "kicked the bucket" faster than "lifted the bucket" by 51ms (Swinney \& Cutler 1979)
- Production latency: German irregular past participle (-n) faster than regular (-t) by 38ms (Clahsen \& Fleischhauer 2011): stem and surface frequencies matched
- This leads to an evaluation metric in the sense of SPE


## Price of Exceptions


$p_{e} T[$ listing $e]+\left(1-p_{e}\right) e$
$<\quad T[$ listing $N]$

## Tipping Point

- Assume word frequencies follow Zipf's law (they really do)
- Maximum \# of exceptions

$$
e \approx \frac{N}{\ln N}
$$



## Filibuster Proof



## Tipping Points

- Productive rules can tolerate few exceptions (sub-linear)
- "-ed" rule is safe ( $\mathrm{M}=120, \mathrm{~N}=800,800 /$ $\ln 800 \approx 120$ )
- Makes predictions about morphological and syntactic productivity (room for individual variation)
- Makes predictions about productivity of rules on purely numerical basis
- See our other papers for details for predictions among morphological productivity, phonological and syntactic acquisition and language change


## Five Case Studies of Gaps

- Most accounts of paradigmatic gaps
- multiple forms so the speaker is at a loss, or some forms are generated but "dispreferred"
- Halle (1973) and Baronian (2005): the gapped forms are not generated (e.g., [-lexical insertion]), but no concrete proposal on why and where gaps occur


## Gaps $=$ Below Tipping Point

- Alternations constitute exceptions for each other
- U-shape curve in past tense acquisition
- Irregulars are initially accurate: the "dip" is caused by the emergence of "-ed" as a productive rule
- Initial verbs are mostly irregulars: the child needs to accumulate enough regulars to know "-ed" is productive
- If there are too many exceptions, everyone is a loser


## Case I: stride

- 150 irregular verbs in English
- A great majority shows preterite $\sim$ past participle syncretism ("brought", "kept", "lost"): 102
- But that's not enough to be extendable: 48 exceptions vs. 30 (150/ $\ln 150$ )
- You must hear it in the input, and if no one says anything, you'll be at a loss too!
- Ditto for *forwent, *sightsaw, ...


## stride-stridden sub-regularity?

- irregular verbs containing /aI/ and coda does not contain a nasal (e.g., find, shine) tend to have /I ... әn/ in past participle
- abide, arise, bite, ?chide, dive, drive, fight, hide, light, ride, override, rise, slide, strike, strive, ?thrive, write
- 17 words can tolerate 6 exceptions
- $/ \mathrm{aI} / \rightarrow / \mathrm{I} \ldots$... $\mathrm{n} /$ for past participle may be on the cusp of productivity but it's clearly not for everyone


## Case II: amn't (23/ln23 = 7)

|  | a. | do | [du] | don't | [dont] |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | b. | does | [d^z] | doesn't | [d^znt] |
|  | c. | did | [did] | didn't | [dıdñt] |
|  | d. | have | [hæv] | haven't | [hævn! $]$ |
|  | e. | has | [hæz] | hasn't | [hæznt] |
|  | f. | had | [hæd] | hadn't | [hædnt] |
|  |  | can | [kæn] | fcannot | [kænat] |
|  | g. | can | [kæn] | \{ can't | [kænt] |
|  | h. | could | [kud] | couldn't | [kudnt] |
|  | i. | may | [me] | - |  |
|  | j. | might | [mait] | mightn't | [maitnt] |
|  | k. | shall | [šæl] | shan't | [šænt] |
|  | 1. | should | [šud] | shouldn't | [ŠUdñt] |
| LWicky \& | m. | will | [wil] | won't | [wont] |
| Pullum | n . | would | [wud] | wouldn't | [wudnt] |
|  | o. | dare | [der] | daren't | [dernt] |
| (1983) | p. | must | [mıst] | mustn't | [masnt] |
|  | q. | need | [nid] | needn't | [nidñt] |
|  | r. | ought | [ t ] | oughtn't | [ t ¢! t ] |
|  | s. | am | [æm] | - | - |
|  | t. | are | [ar] | aren't | [arnt] |
|  | u. | is | [Iz] | isn't | [ızñt] |
|  | v . | was | [wnz] | wasn't | [wıznt] |
|  | w. | were | [wr] | weren't | [wront] |

## Case III: Spanish

- In some Spanish verbs, an unstressed $e$ or $o$ in the final root syllable becomes ie [je] and ue [we] under primary stress: diphthongization (Harris 1969)

| conjugatio | no change | e-ie, o-ue | $\mathbf{N}$ | threshold |
| :---: | :---: | :---: | :---: | :---: |
| first (-ar) | $\mathbf{1 0 5 0}$ | 125 | 1175 | $166($ yes $)$ |
| second (- | $\mathbf{1 8 9}$ | 29 | 218 | $42($ yes $)$ |
| third (-ir) | $\mathbf{1 9}$ | 33 | 52 | $13($ no $)$ |

- No change is the default in 1st and 2nd, and that's how children over-regularize (Clahsen et al. 2002, Mayol 2007)
- Third conjugation has no default and that's where gaps are found (e.g., abolir-*abolo/*abuelo 'abolish', colorir-*coloro/*coluero 'colorize'; Real Academia Española 1992)


## A Comparison

- Albright (2003): an inductive generalization model (Albright \& Hayes 2002, see also Chomsky 1955, Mitchell 1982)
- Claims correlation both model confidence and speaker judgment
- Tested on 3rd conjugation roots
- Confidence does not correlate with gaps or attested forms



## Case IV: Polish

- Polish singular masculine genitives take either $-a$ or $-u$ as suffix but neither seems to be the default based on a suite of tests.
- Plurals take -ow as the default, with exceptional -i/y suffix
- Posed as a challenge to the dual route model of morphology in favor of all storage/usage via token frequency (Dabrowska 2001)
- Analysis of child-directed Polish in CHILDES

| suffix | type freq. | productive? | ave. token freq. | error $\%$ |
| :---: | :---: | :---: | :---: | :---: |
| $-\mathrm{a}(\mathrm{sg})$. | $\mathbf{8 3 7}$ | no | 7.17 | $1.28 \%$ |
| $-\mathrm{u}(\mathrm{sg})$. | $\mathbf{5 1 6}$ | no | 8.8 | $0.24 \%$ |
| - ow (pl.) | $\mathbf{5 5 1}$ | yes | 6.5 | $0.41 \%$ |
| $-\mathrm{i} / \mathrm{y}$ (pl.) | $\mathbf{6 1}$ | no | 11.4 | $\mathbf{1 5 . 5 3} \%$ |

predict gaps and default, and rejects the pure frequency account

## Case V: Russian

- Root final $t$ of many verbs in Russian 2nd conjugation is realized as č in the 1sg. non-past
- but many instead mutate to šj (smutit'-smušju/'confuse') or have a gap (očutit'sja- *očučus'/*očušjus' 'find oneself')
- Counting Russian National Corpus words ( $>1$ per million)
- 59 verbs of this type, 19 following the minority pattern
- $19>59 / \ln 59=14$


## Summary

- Gaps arise when productivity fails (Halle 1973), and productivity fails when $\mathbf{e}>\mathbf{N} / \ln \mathbf{N}$
- More general, a predictive model of productivity can keep exceptions at bay: the core grammar is not threatened, and evaluation metrics still have shelf life.

